## **Permutations**

## **Detailed Examples**

## Main Ideas

Permutations are easy to calculate. The easiest way is to remember the multiplication rule for counting and using the permutation pattern. The formula for permutations makes this harder than it needs to be.

## Example 7.6

Find the following numbers:

- 1. The number of permutations of 12 objects taken 3 at a time
- 2. The number of permutations of 8 objects taken 5 at a time
- 3. The number of permutations of 32 objects taken 2 at a time

Work

Steps Start with a slot diagram. Because there are three objects, use three slots.

1<sup>st</sup>Object 2<sup>nd</sup>Object 3<sup>rd</sup>Object

Steps Work There are 12 possibilities for the first choice. Put a 12 in the first slot.

2 1<sup>st</sup>Object 2<sup>nd</sup>Object 3<sup>rd</sup>Object |21<sup>st</sup>Object 2<sup>nd</sup>Object 3<sup>rd</sup>Object 1<sup>st</sup>Object 2<sup>nd</sup>Object 3<sup>rd</sup>Object

There are 11 possibilities for the second objects. That is because we chose one of the 12 objects in the first step. Put an 11 in the second slot.

Fill the remaining slots with decreasing numbers.

Work

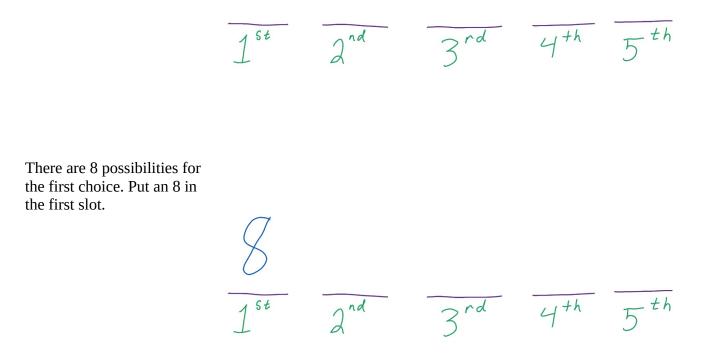
Steps Multiply the numbers.

12 × 11 × 10 1<sup>st</sup>Object 2<sup>nd</sup>Object 3<sup>rd</sup>Object = 1320

The number of permutations of 12 objects taken 3 at a time is 1,320. Our notation for this permutation is

 $_{12}P_{3}$ .

StepsWorkStart with a slot diagram.Because there are five<br/>objects, use five slots.



Steps Work There are 7 possibilities for the second objects. That is because we chose one of the 8 objects in the first step. Put a 7 in the second slot.  $I = \frac{5t}{2} = \frac{3^{rd}}{3^{rd}} = \frac{3^{rd}}{4^{rh}}$ 

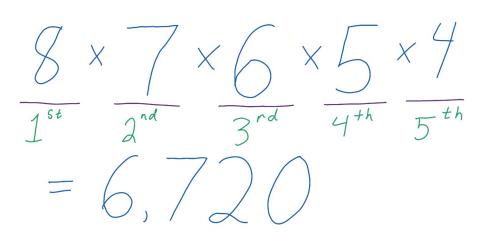
Fill the remaining slots with decreasing numbers.

 $\frac{8}{1^{5t}} \frac{7}{2^{nd}} \frac{6}{3^{rd}} \frac{5}{4^{+h}} \frac{4}{5^{th}}$ 

th

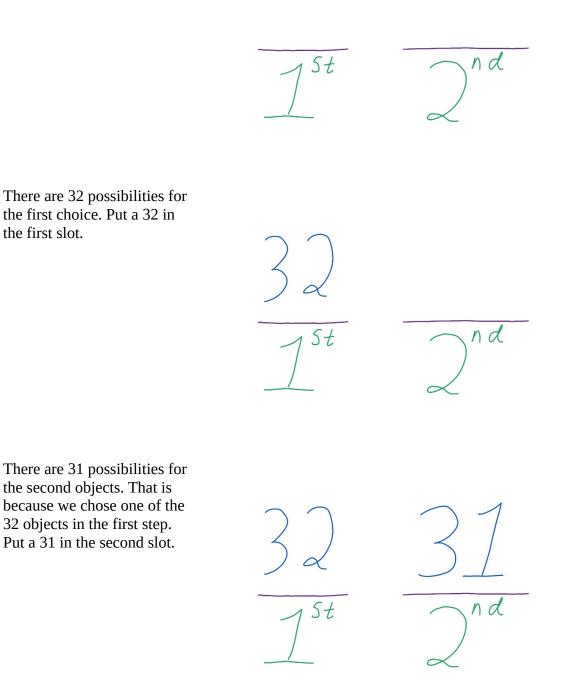
5

Multiply the numbers.

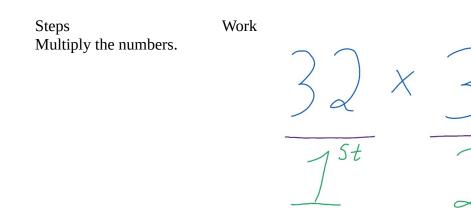


The number of permutations of 8 objects taken 5 at a time is 6,720. Our notation for this permutation is  ${}_{8}P_{5}$ .

Steps Start with a slot diagram. Because there are three objects, use three slots. Work



Access for free at https://openstax.org/books/contemporary-mathematics/pages/1-introduction



The number of permutations of 32 objects taken 2 at a time is 992. Our notation for this permutation is  ${}_{32}P_2$ .

nd